

## Relación 10: Deducción natural en la LPO

Demostrar mediante deducción natural

1.  $\forall x[P(x) \rightarrow \exists yQ(y)],$   
 $\vdash \forall x\exists y[P(x) \rightarrow Q(y)]$
2.  $\forall x[P(x) \rightarrow \neg C(x)],$   
 $\exists x[C(x) \wedge B(x)]$   
 $\vdash \exists x[B(x) \wedge \neg P(x)]$
3.  $\forall x\exists y[P(x) \rightarrow Q(y)]$   
 $\vdash \forall x[P(x) \rightarrow \exists yQ(y)]$
4.  $\forall x\forall y[(\exists zR(y, z)) \rightarrow R(x, y)],$   
 $\exists x\exists yR(x, y)$   
 $\vdash \forall x\forall yR(x, y)$